# Mendel's Principles of Heredity

## **Synopsis**

Chapter 1 covers the basic principles of inheritance that can be summarized as Mendel's Laws of Segregation (for one gene) and Independent Assortment (for more than one gene).

## Key terms

- **genes** and **alleles** of genes A gene determines a trait, and different alleles or forms of a gene exist. The color gene in peas has two alleles: yellow and green.
- **genotype** and **phenotype** Genotype is the genetic makeup of an organism (written as alleles of specific genes), while phenotype is how the organism looks.
- **homozygous** and **heterozygous** When both alleles of a gene are the same, the individual is homozygous for that gene (or **pure breeding**). If the two alleles are different, the organism is heterozygous (also called a **hybrid**).
- **dominant** and **recessive** The dominant allele is the one that controls phenotype in the heterozygous genotype; the recessive allele controls phenotype only in a homozygote.
- **monohybrid** or **dihybrid cross** a cross between individuals who are both heterozygotes for one gene (monohybrid) or for two genes (dihybrid).
- **testcross** performed to determine if an individual with the dominant characteristic is homozygous or heterozygous: An individual with the dominant phenotype but unknown genotype is crossed with an individual with the recessive phenotype.

## **Key ratios**

**3:1** – Ratio of progeny phenotypes in a cross between monohybrids

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[Aa \times Aa \rightarrow 3 A - (dominant phenotype) : 1 aa (recessive phenotype)]
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1:2:1 – Ratio of progeny genotypes in a cross between monohybrids

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(Aa \times Aa \rightarrow 1 AA : 2 Aa : 1aa)
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- 1:1 Ratio of progeny genotypes in a cross between a heterozygote and a recessive homozygote  $(Aa \times aa \rightarrow 1 \ Aa : 1aa)$
- 1:0 All progeny are the same phenotype. Can result from either of two cases:

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[AA \times -- \rightarrow A – (all dominant phenotype)]
[aa \times aa \rightarrow aa (all recessive phenotype)]
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9:3:3:1 – Ratio of progeny phenotypes in a dihybrid cross

 $(Aa Bb \times Aa Bb \rightarrow 9 A-B-: 3 A-bb: 3 aa B-: 1 aa bb)$ 

## **Problem Solving**

The essential component of solving most genetics problems is to DIAGRAM THE CROSS in a consistent manner. Usually you will be given information about phenotypes, so the diagram would be:

Phenotype of one parent  $\times$  phenotype of the other parent  $\rightarrow$  phenotype(s) of progeny

The goal is to assign genotypes to the parents and then use these predicted genotypes to generate the genotypes, phenotypes, and ratios of progeny. If the predicted progeny match the observed data you were provided, then your genetic explanation is plausible.

The points listed below will be particularly helpful in guiding your problem solving:

- Remember that two alleles of each gene exist when describing the genotypes of individuals. But if you are describing gametes, remember that only one allele of each gene is in a gamete.
- You will need to determine whether a character is dominant or recessive. Two main clues will help you answer this question.
  - $\circ$  First, if the parents of a cross are true breeding for the alternative characters of the trait, look at the phenotype of the F<sub>1</sub> progeny. Their genotype must be heterozygous, and their phenotype is thus determined by the dominant allele of the gene.
  - Second, look at the F<sub>2</sub> progeny (that is, the progeny of the F<sub>1</sub> hybrids). The 3/4 portion of the 3:1 phenotypic ratio indicates the dominant character.
- You should **recognize the need to set up a testcross** (to establish the genotype of an individual showing the dominant character by crossing this individual to a homozygote for the recessive allele).
- You must keep in mind the basic rules of probability:
  - Product rule: If two outcomes must occur together as the result of independent events, the probability of one outcome AND the other outcome is the product of the two individual probabilities.
  - o *Sum rule:* If there is more than one way in which an outcome can be produced, the probability of one OR the other occurring is the sum of the two mutually exclusive individual probabilities.
- Be aware that sometimes you need to use **conditional probability**, meaning that an event's probability is influenced by its relationship to another event that has already occurred. You were introduced to conditional probability in Solved Problem III in this chapter, and several of the problems in Section 1.3 require this kind of thinking. For example, suppose you are given a pedigree diagram for a disease caused by a recessive allele. You are asked to determine the chance that an unaffected individual is a carrier (*Dd*), when both parents are carriers. As the cross that produced the unaffected individual is  $Dd \times Dd$ , you would expect the chance of a Dd child to be 1/2. This is true, but it was not the question you were asked! You know something about the individual in question—which is that they are unaffected—they cannot be dd. This means that in this case, the 1 DD: 2 Dd: 1 dd ratio changes to 1 DD: 2 Dd, and the chance is 2/3 that the unaffected individual is a carrier. When solving probability problems in pedigrees,

- always think carefully about what you know (and what you don't know) about each individual.
- Remember that Punnett squares are not the only means of analyzing a cross; branched-line diagrams and calculations of probabilities using the product and sum rules are more efficient ways of looking at complicated crosses involving more than one or two genes.
- You should be able to draw and interpret pedigrees. When the trait is rare, look for vertical patterns of inheritance characteristic of dominant traits, and horizontal patterns that typify recessive traits. Check your work by assigning genotypes to all individuals in the pedigree and verifying that these make sense.
- The vocabulary problem (the first problem in the set) is a useful gauge of how well you know the terms most crucial for your understanding of the chapter.

## **Vocabulary**

#### 1.

a.	phenotype	4.	observable characteristic
b.	alleles	3.	alternate forms of a gene
c.	independent assortment	6.	alleles of one gene separate into gametes randomly with respect to alleles of other genes
d.	gametes	7.	reproductive cells containing only one copy of each gene
e.	gene	11.	the heritable entity that determines a characteristic
f.	segregation	13.	the separation of the two alleles of a gene into different gametes
g.	heterozygote	10.	an individual with two different alleles of a gene
h.	dominant	2.	the allele expressed in the phenotype of the heterozygote
i.	F <sub>1</sub>	14.	offspring of the P generation
j.	testcross	9.	the cross of an individual of ambiguous genotype with a homozygous recessive individual
k.	genotype	12.	the alleles an individual has
1.	recessive	8.	the allele that does not contribute to the phenotype of the heterozygote
m.	dihybrid cross	5.	a cross between individuals both heterozygous for two genes
n.	homozygote	1.	having two identical alleles of a given gene

#### Section 1.1

2. Prior to Mendel, people held two basic misconceptions about inheritance. First was the common idea of blended inheritance: that the parental characteristics become mixed in the offspring and forever changed. Second, many people thought that one parent contributes the most to an offspring's inherited features. (For example, some people thought they saw a fully formed child in a human sperm.)

In addition, **people who studied inheritance did not approach the problem in an organized way.** They did not always control their crosses. They did not look at traits with clear-cut alternative characteristics. They did not start with pure-breeding lines. They did not count the progeny types in their crosses. For these reasons, they could not develop the same insights as did Mendel.

#### 3. Several advantages exist for using peas for the study of inheritance:

- Peas have a fairly rapid generation time (at least two generations per year if grown in the field, three or four generations per year if grown in greenhouses).
- Peas can either self-fertilize or be crossed artificially by an experimenter.
- Peas produce large numbers of offspring (hundreds per parent).
- Peas can be maintained as pure-breeding lines, simplifying the ability to perform subsequent crosses.
- Because peas have been maintained as inbred stocks, two easily distinguished and discrete forms of many traits are known.
- Peas are easy and inexpensive to grow.

#### In contrast, studying genetics in humans has several disadvantages:

- The generation time of humans is very long (roughly 20 years).
- No self-fertilization occurs in humans, and it is not ethical to manipulate crosses.
- Humans produce only a small number of offspring per mating (usually only one) or per parent (almost always fewer than 20).
- Although people who are homozygous for a trait do exist (analogous to purebreeding stocks), homozygosity cannot be maintained because mating with another individual is needed to produce the next generation.
- Because human populations are not inbred, most human traits show a continuum of phenotypes; only a few traits have two distinct forms.
- People require a lot of expensive care to "grow".

One major advantage exists nonetheless for the study of genetics in humans: Because many inherited traits result in disease syndromes, and because the world's population now exceeds 7 billion people, a very large number of people with diverse, variant phenotypes can be recognized. These variations are the raw material of genetic analysis.

#### Section 1.2

- **4. a.** Two phenotypes are seen in the second generation of this cross: normal and albino. Thus, only one gene with two alleles is needed to control the phenotypes observed. The 3:1 ratio of these phenotypes in the F<sub>2</sub> generation will be seen only if a single gene is involved.
  - **b.** Note that the phenotype of the first generation progeny is normal color, and that in the second generation, there is a ratio of 3 normal : 1 albino. Both observations show that the allele controlling the normal phenotype (*A*) is dominant to the allele controlling the albino phenotype (*a*).
  - **C.** In a testcross, an individual showing the dominant phenotype but that has an unknown genotype (the normal-colored female parent in this problem) is mated with an individual that shows the recessive phenotype and is therefore homozygous for the recessive allele. In this case, the individual with the recessive phenotype must be both male and an albino, so **the male parent's genotype is aa.** The normally colored offspring must receive an *A* allele from the mother, so **the genotype of the normal offspring of the testcross is** *Aa.* The albino offspring must receive an *a* allele from the mother, so **the genotype of the albino offspring of the testcross is** *aa.* Thus, **the female parent must be heterozygous** *Aa.*
- 5. Because two different phenotypes result from the mating of two cats of the same phenotype, and because the ratio of the short-haired to long-haired progeny is 3:1, only a single gene is involved, and the short-haired parent cats must have been heterozygous. The phenotype expressed in the heterozygotes (the parent cats) is the dominant phenotype. Therefore, short hair is dominant to long hair.
- **6. a.** Two affected individuals have an affected child and a normal child. This outcome is not possible if the affected individuals were homozygous for a recessive allele conferring piebald spotting, and if the trait is controlled by a single gene. Therefore, **piebald must be the dominant characteristic.** 
  - **b.** If the trait is dominant, the piebald parents could be either homozygous (PP) or heterozygous (Pp). However, because the two affected individuals have an unaffected child (pp), they both must be heterozygous (Pp). A diagram of the cross follows:

piebald 
$$\times$$
 piebald  $\rightarrow$  1 piebald : 1 normal  $Pp$   $Pp$   $Pp$   $pp$ 

Note that although the apparent ratio is 1:1, this is not a testcross but is instead a cross between two monohybrids. The reason for this discrepancy is that only two progeny were obtained, so this number is insufficient to establish what the true ratio would be (it should be 3:1) if many progeny resulted from the mating.

7. You would conduct a testcross between your normal-winged fly (*W*–) and a short-winged fly that must be homozygous recessive (*ww*). The possible results are diagrammed here; the first genotype in each cross is that of the normal-winged fly whose genotype was originally unknown. Note that if the normal-winged fly is a homozygote,

all the progeny should have normal wings, but if the normal-winged fly is a heterozygote, half the progeny should have normal wings and the other half should have short wings.

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WW \times ww \rightarrow \text{all } Ww \text{ (normal wings)}

Ww \times ww \rightarrow 1/2 \ Ww \text{ (normal wings)} : 1/2 \ ww \text{ (short wings)}
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**8.** First diagram the crosses:

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closed \times open \rightarrow F<sub>1</sub> all open \rightarrow F<sub>2</sub> 145 open : 59 closed F<sub>1</sub> open \times closed \rightarrow 81 open : 77 closed
```

The results of the crosses fit the pattern of inheritance of a single gene, with open being dominant to closed. The first cross is similar to those Mendel did with purebreeding parents, although you were not provided with the information that the starting plants were true-breeding. The  $F_1$  plants are open, indicating that open is dominant. The closed parent must be homozygous for the recessive allele. Because only one phenotype is seen among the  $F_1$  plants, the open parent must be homozygous for the dominant allele. Thus, the parental cucumber plants were indeed true-breeding homozygotes.

Self-fertilization of the  $F_1$  plants results in a 3:1 ratio of open: closed among the  $F_2$  progeny. The 3:1 ratio in the  $F_2$  shows that a single gene controls the trait and that the  $F_1$  plants are all monohybrids (that is, they are heterozygotes).

The final cross verifies that the  $F_1$  plants from the first cross are heterozygtes because **this testcross yields a 1:1 ratio of open: closed progeny.** In summary, all the data are consistent with the trait being determined by one gene with two alleles, and open being the dominant characteristic. Rewritten as genotypes for a gene with alleles O and O, the crosses were:

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oo (closed) \times OO (open) \rightarrow F_1 Oo (open) \rightarrow F_2 145 O- (open): 59 oo (closed) F_1 Oo (open) \times oo (closed) \rightarrow 81 Oo (open): 77 oo (closed)
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9. The dominant characteristic (short tail) is easier to eliminate from the population by selective breeding. The reason is you can recognize every animal that has inherited the *short tail* allele, because only one such dominant allele is needed to see the characteristic. If you prevent all the short-tailed animals from mating, then the allele would become extinct.

On the other hand, the recessive *dilute* allele can be passed unrecognized from generation to generation in heterozygous mice (who are *carriers*). The heterozygous mice are not dilute, so they cannot be distinguished from homozygous dominant mice with normal coat color. You could prevent the homozygous recessive mice with the dilute characteristic from mating, but the *dilute* allele would remain among the carriers, which you could not recognize.

10. The problem states that only one gene is involved in this trait, and that the dominant allele is dimpled (D) while the recessive allele is nondimpled (d). (We are using Mendelian symbols here instead of human symbols for genotypes to emphasize which allele is dominant and which is recessive.)

**a**. Diagram the cross described in this part of the problem:

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nondimpled \delta \times \text{dimpled } Q \rightarrow \text{proportion of dimpled } F_1?
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Note that the dimpled woman in this cross had a *dd* (nondimpled) mother, so the dimpled woman MUST be heterozygous. We can thus rediagram this cross with genotypes:

dd (nondimpled)  $\eth \times Dd$  (dimpled)  $Q \to 1/2 \, Dd$  (dimpled) :  $1/2 \, dd$  (nondimpled) One half of the children produced by this couple would be dimpled.

**b.** Diagram the cross:

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dimpled (D?) \circlearrowleft \times \text{ nondimpled } (dd) \circlearrowleft \rightarrow \text{ nondimpled } F_1(dd)
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Because they have a nondimpled child (dd), the man must have a d allele to contribute to the offspring. The man is thus of genotype Dd.

**C.** Diagram the cross:

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dimpled (D?) \circlearrowleft \times \text{ nondimpled } (dd) \circlearrowleft \to 8 \text{ F}_1, \text{ all dimpled } (D-)
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The D allele in the children must come from their father. The father could be either DD or Dd, but it is most probable that the father's genotype is DD. We cannot rule out completely that the father is a Dd heterozygote. However, if this was the case, the probability that all 8 children would inherit the D allele from a Dd parent is only  $(1/2)^8 = 1/256$ .

- 11.  $\alpha$ . The 3:1 ratio in the progeny of cross  $1 \times 4$  suggests that a single gene controls flowering time, and that late (F) is dominant to early (f).
  - **Plants 1 and 4 are** Ff because their progeny exhibit a 3 late (F-):1 early (ff) ratio. **Plant 2 is** ff because when crossed with plant 1  $(Ff \times ff)$ , the progeny are in a 1:1 ratio of late (Ff) to early (ff). **Plant 3 is** FF because when crossed with either 1, 3, or 4, all the progeny are late (F-).
  - **c.** Selfing of Plant 1 or Plant 4 (Ff) would produce progeny in a phenotypic ratio of 3 late: 1 early (3 F-:1 ff). Selfing of Plant 2 (ff) would produce all early (ff) progeny, and selfing of Plant 3 would result in progeny that are all late (FF).
- **12. a.** You need to realize that the results tabulated are unlike those of the plants in the previous problem in an important way: The parents are not two individuals who had 30–50 progeny. Instead, the entries in the table show the progeny of many pairs of parents with the same characteristics, but who could have different genotypes. This means that if sticky and dry are controlled by alternate alleles of a single gene, in any row of the table involving parents with the dominant phenotype, those parents could actually be a mixture of homozygous dominant and heterozygous individuals.

Thus, in a row where both parents have the dominant phenotype, some of the crosses could be  $Ss \times Ss$ , while in a row where one parent has the dominant phenotype and the other parent has the recessive phenotype, some of the crosses could be  $Ss \times ss$ . Both cases could produce some progeny who will be homozygous recessive (ss). Only crosses between two homozygous recessive individuals will result in progeny that all have the recessive phenotype. The only crosses that fit this

criterion are in the row: dry  $\times$  dry  $\rightarrow$  all dry. Therefore, dry is the recessive phenotype (ss) and sticky is the dominant phenotype (S-).

b. 3:1 or 1:1 ratios are not observed in the table because some sticky individuals in each of the first two rows are SS while others are Ss.

In the first row of the table, the sticky  $\times$  sticky matings in this human population are not simply crosses between heterozygotes, but instead a mix of three different kinds of matings: between two heterozygotes ( $SS \times SS$ ), between two homozygotes ( $SS \times SS$ ), and between a homozygote and heterozygote ( $SS \times SS$ ). The progeny from the two latter crosses obscure the 3:1 ratio that would result from crosses between heterozygotes.

In the second row of the table, the sticky  $\times$  dry matings include both  $Ss \times ss$  and  $SS \times ss$ . The progeny of the latter crosses obscure the 1:1 ratio that would result from any  $Ss \times ss$  testcrosses in the same row.

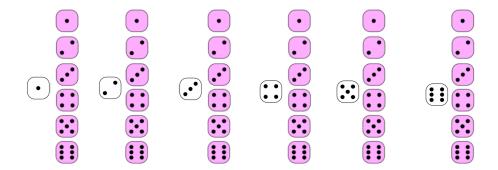
**13.** Diagram the cross:

black  $\times$  red  $\rightarrow$  1 black: 1 red

No, you cannot tell how coat color is inherited from the results of this one mating. The 1:1 ratio indicates that this was a testcross—a cross between a heterozygote and a homozygous recessive. However, we cannot know from the testcross whether red or black is the dominant phenotype. To determine which phenotype is dominant, remember that an animal with a recessive phenotype must be homozygous. Thus, if you mate several red horses to each other and also mate several black horses to each other, the crosses that always yield only offspring with the parental phenotype must have been between homozygous recessives. For example, if all the black  $\times$  black matings result in only black offspring, black is recessive. Some of the red  $\times$  red crosses (that is, crosses between heterozygotes) would then result in both red and black offspring in a ratio of 3:1. To establish this point, you might have to do several red  $\times$  red crosses, because some of these crosses could be between red horses homozygous for the dominant allele. You could of course ensure that you were sampling heterozygotes by using the progeny of black  $\times$  red crosses (such as that described in the problem) for subsequent [black  $\times$  black] or [red  $\times$  red] crosses.

- **14. a. 1/6** because a die has 6 different sides.
  - **b.** Three even numbers exist (2, 4, and 6). The probability of obtaining any one of these is 1/6. Because the 3 events are mutually exclusive, use the sum rule: 1/6 + 1/6 + 1/6 = 3/6 = 1/2.
  - C. You must roll either a 3 or a 6, so 1/6 + 1/6 = 2/6 = 1/3.

When thinking about probabilities involving 2 dice (in the diagram that follows, a *white* one and a *pink* one), it helps to realize that: (1) The probabilities calculated for rolling both dice simultaneously will be the same as those calculated for rolling them in succession (first one, then the other), and (2) as shown in the diagram that follows, 36 different outcomes are possible:



- **d.** Each die is independent of the other, thus the product rule is used:  $1/6 \times 1/6 = 1/36$ . (Two 6s is one of the 36 possible outcomes.)
- **e.** The probability of getting an even number on one die is 3/6 = 1/2 [see part (b)]. This is also the probability of getting an odd number on the second die. This result could happen either of 2 ways—you could get the odd number first and the even number second, or vice versa, and these are mutually exclusive possibilities. Thus, the probability of both occurring is  $(1/2 \times 1/2) + (1/2 \times 1/2) = 1/4 + 1/4 = 1/2$ .

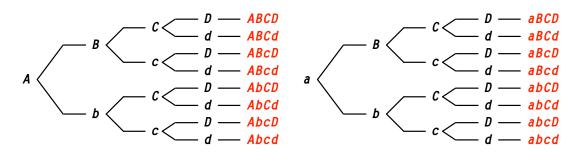
Another way of thinking about this problem is that the first die can land any way (probability = 1), but the second die must show an odd number (probability = 1/2) if the first die was even, and an even number (probability = 1/2) if the first die was odd. Therefore, no matter how the first die lands, the second die has a 1/2 chance of landing on a number that satisfies the stated criterion, and so the probability that the criterion is satisfied is  $1 \times 1/2 = 1/2$ . (You can see in the diagram above that 18 of the 36 possible outcomes satisfy the criterion that one die has an odd number and the other die has an even number.)

The probability of any specific number on a die = 1/6. The probability of the same number on the other die = 1/6. The probability of both occurring at same time is  $1/6 \times 1/6 = 1/36$ . The same probability is true for the other 5 possible numbers on the dice. Thus, the probability of any of these mutually exclusive situations occurring is 1/36 + 1/36 + 1/36 + 1/36 + 1/36 + 1/36 = 6/36 = 1/6.

Another way of thinking of about this problem is that the first die can land any way at all (probability = 1), but the second die must match the first one (probability = 1/6). The chance of both events happening is  $1 \times 1/6 = 1/6$ . (In other words, 6 of the 36 possible outcomes satisfy the criterion that both numbers are the same.)

- **g.** The probability of getting two numbers both over four is the probability of getting a 5 or 6 on one die (1/6 + 1/6 = 1/3) and a 5 or 6 on the other die (1/3). The results for the two dice are independent events, so  $1/3 \times 1/3 = 1/9$ . (In other words, 4 of the 36 possible outcomes satisfy the criterion both numbers are over 4.)
- 15. a. The probability of drawing a face card = 0.23 (= 12 face cards / 52 cards). The probability of drawing a red card = 0.5 (= 26 red cards / 52 cards). The probability of drawing a red face card = probability of a red card × probability of a face card = 0.23 × 0.5 = 0.12. (Alternatively, 6 red face cards / 52 cards = 0.12.)

- **b.** As seen in part (a), the probability of drawing a face card in a deck of 52 cards is 0.23. If after each draw, the card is returned to the deck, then the deck will have 52 cards in each draw. Thus, the chance that all four cards picked are face cards is  $(0.23)^4 \approx 0.0028$ .
- C. The chance that the first card is a face card is (12/52). If that card was a face card, then the chance that the second card is a face card is (11/51), the chance that the third card is also a face card is (10/50), and the chance that the fourth card is a face card is (9/49). (This is an example of conditional probability, because the probabilities change after each draw.) Thus, if the cards are not returned to the deck, the chance that the first four cards picked are face cards is  $(12/52) \times (11/51) \times (10/50) \times (9/49) \approx 0.0018$ .
- **16. a.** The  $Aa\ bb\ CC\ DD$  woman can produce 2 genetically different eggs that vary in their allele of the first gene  $(A\ or\ a)$ . She is homozygous for the other 3 genes and can only make eggs with the  $b\ C\ D$  alleles for these genes. Thus, using the product rule (because the inheritance of each gene is independent), she can make  $2\times 1\times 1\times 1=2$  different types of gametes:  $(A\ b\ C\ D)$  and  $a\ b\ C\ D$ .
  - **b.** Using the same logic, an  $AA \ Bb \ Cc \ dd$  woman can produce  $1 \times 2 \times 2 \times 1 = 4$  different types of gametes:  $A \ (B \ or \ b) \ (C \ or \ c) \ d$ .
  - C. A woman of genotype  $Aa\ Bb\ cc\ Dd$  can make  $2\times 2\times 1\times 2=8$  different types of gametes:  $(A\ or\ a)\ (B\ or\ b)\ c\ (D\ or\ d)$ .
  - **d.** A woman who is a quadruple heterozygote can make  $2 \times 2 \times 2 \times 2 = 16$  different types of gametes: (A or a) (B or b) (C or c) (D or d). This problem [like those in parts (a–c) above] can also be visualized with a branched-line diagram.



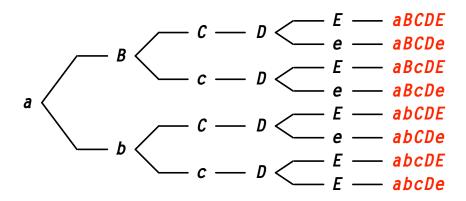
17. *a.* The probability of any particular progeny phenotype in this cross depends only on the gamete from the heterozygous parent. The reason is that the homozygous recessive parent always provides a gamete with all recessive alleles  $(a \ b \ c \ d)$ . The probability that a child will resemble the quadruply heterozygous parent is thus:  $1/2A \times 1/2B \times 1/2C \times 1/2D = 1/16$ . The probability that a child will resemble the quadruply homozygous recessive parent is:  $1/2a \times 1/2b \times 1/2c \times 1/2d = 1/16$ . The probability that a child will resemble either parent is then 1/16 + 1/16 = 1/8. This cross will produce 2 different characters for each gene or  $2 \times 2 \times 2 \times 2 = 16$  potential phenotypes.

- b. The probability of a child resembling the recessive parent is 0; the probability of a child resembling the dominant parent is  $1 \times 1 \times 1 \times 1 = 1$ . The probability that a child will resemble one of the two parents is 0 + 1 = 1. Only one phenotype is possible in the progeny (dominant for all 4 genes), as  $(1)^4 = 1$ .
- C. The probability that a child would show the dominant character for any one gene is 3/4 in this sort of cross (remember the 3:1 phenotypic ratio in the progeny of monohybrid crosses), so the probability of resembling the parent for the traits associated with all four genes is  $(3/4)^4 = 81/256$ . Two characters are possible for each gene, so  $(2)^4 = 16$  different kinds of progeny.
- **d.** All progeny will resemble their parents because all the alleles from both parents are identical, so the probability = 1. Only one phenotype is possible for each gene in this cross; because  $(1)^4 = 1$ , the child can have only one possible phenotype when considering all four genes.
- **18. a.** The combination of alleles in the egg and sperm allows only one genotype for the zygote: **aa Bb Cc DD Ee**.
  - **b.** Because the inheritance of each gene is independent, you can use the product rule to determine the number of different gamete types possible:

 $1 \times 2 \times 2 \times 1 \times 2 = 8$  types of gametes. To figure out the genotypes of these gametes, consider the possibilities for each gene separately and then the possible combinations of genes in a consistent order. For each gene the possibilities are:

a, (B:b), (C:c), D, and (E:e). The possibilities can be determined using the product rule. Thus, for the first 2 genes  $[a] \times [B:b]$  gives [a B:a b]. Next,  $[a B:a b] \times [C:c]$  gives [a B C:a Bc:a bC:a bC:a bc]. Next,  $[a B C:a Bc:a bC:a bc] \times [D]$  gives [a B CD:a BcD:a bCD:a bcD]. And finally, [a B CD:a BcD:a bCDE:(ii) a bCDE:(vii) a bCDE:(viii) a bCDE:(viii) a bCDE].

This problem can also be visualized with a branched-line diagram:



- 19. Your friend is wrong. As each of these triplets is an independent event, we use the product rule to determine the probability of 3 boys:  $P(BBB) = 1/2 \times 1/2 \times 1/2 = 1/8$ . The probability of 3 girls is the same: P(GGG) = 1/8. However, the probability of 2 boys and 1 girl is greater than 1/8 because it includes three different birth orders—BBG, BGB, GBB—each with a probability of 1/8. Thus, we use the sum rule to determine the probability of 2 boys and 1 girl in any order: 1/8 + 1/8 + 1/8 = 3/8. The same logic applies to two girls and a boy, the probability of which is also 3/8. Notice that because 3 boys, 3 girls, 2 boys + 1 girl, and 2 girls + 1 boy are the only options, the sum of their individual probabilities is 1 (that is, 1/8 + 1/8 + 3/8 + 3/8 = 1).
- **20.** The first two parts of this problem involve the probability of occurrence of two independent traits: the sex of a child and galactosemia. The parents are heterozygous for galactosemia, so a 1/4 chance exists that a child will be affected (that is, homozygous recessive). The probability that a child is a girl is 1/2. The probability of an affected girl is therefore  $1/2 \times 1/4 = 1/8$ .
  - **G.** Fraternal (nonidentical) twins result from two independent fertilizations and therefore, the probability that both will be girls with galactosemia is the product of their individual probabilities (see above);  $1/8 \times 1/8 = 1/64$ .
  - **b.** For identical twins, one fertilization gave rise to two individuals. The probability that both are girls with galactosemia is 1/8.

For parts c–g, remember that each child is an independent fertilization. The sex of the children is not an issue in these parts of the problem.

- **C.** Both parents are carriers (heterozygous), so the probability of having an unaffected child is 3/4. The probability of 4 unaffected children is  $3/4 \times 3/4 \times 3/4 \times 3/4 \times 3/4 = 81/256$ .
- **cf.** The probability that at least one child is affected is the chance of all possible outcomes except the one mentioned in part (c). Thus, the probability is 1 81/256 = 175/256. Note that this general strategy for solving problems, where you first calculate the probability of all outcomes except the one of interest, and then subtract that number from 1, is often useful for problems where direct calculation of the probability of interest is difficult.
- **e.** The probability of an affected child is 1/4 while the probability of an unaffected child is 3/4. Therefore,  $1/4 \times 1/4 \times 3/4 \times 3/4 = 9/256$ .
- f. The probability of 2 affected children and 1 unaffected child in any one particular birth order is  $1/4 \times 1/4 \times 3/4 = 3/64$ . There are 3 mutually exclusive birth orders that could produce 2 affected children and 1 unaffected child—unaffected child first born, unaffected child second born, and unaffected child third born. Thus, the chance that 2 out of 3 children will be affected is 3/64 + 3/64 = 9/64.
- **g.** The genotype of any particular child is independent of all others, so the probability of an affected child is 1/4.
- **21.** Diagram the cross, where *P* is the normal pigmentation allele and *p* is the albino allele: normal  $(P?) \times \text{normal}(P?) \rightarrow \text{albino}(pp)$

An albino must be homozygous recessive pp. The parents are normal in pigmentation and therefore could be PP or Pp. Because they have an albino child, both parents must be carriers (Pp). The probability that their next child will be pp is therefore 1/4.

#### **22.** Diagram the cross:

yellow round × yellow round → 156 yellow round : 54 yellow wrinkled

The ratio for seed shape is 156 round: 54 wrinkled = 3 round: 1 wrinkled. The parents must therefore have been heterozygous (Rr) for the pea shape gene. All the offspring are yellow and therefore are Yy or YY. The parent plants were  $Y-Rr \times YYRr$ . Because no green (yy) progeny exist, you know at least one of the parents must have been YY.

### **23.** Diagram the cross:

smooth black  $\delta \times \text{rough white } Q \to F_1 \text{ rough black}$ 

- → F<sub>2</sub> 8 smooth white : 25 smooth black : 23 rough white : 69 rough black
- **G.** The 9:3:3:1 phenotypic ratio in the  $F_2$  gives away the answer to this problem. This  $F_2$  ratio tells you that the  $F_1$  must be dihybrids, and that rough and black are dominant to smooth and white. Let's use the following symbols: R = rough, r = smooth; B = black, b = white. The  $F_1$  are thus Rr Bb, and because all the  $F_1$  have the same phenotype, the parents must have been homozygotes: rr BB (smooth, black) and RR bb (rough, white). The  $F_2$  are: R B (rough black), R bb (rough white), rr BB (smooth black), and rr bb (smooth white).
- **b.** An  $F_1$  male is heterozygous for both genes (RrBb). The smooth white  $F_2$  female must be homozygous recessive (rrbb). Thus,  $RrBb \times rrbb \rightarrow 1/2 Rr$  (rough): 1/2 rr (smooth) and 1/2 Bb (black): 1/2 bb (white). The inheritance of these genes is independent, so apply the product rule to find the expected phenotypic ratios among the progeny: 1/4 rough black (RrBb): 1/4 rough white (Rrbb): 1/4 smooth black (RrBb): 1/4 smooth white (Rrbb).

#### **24.** Diagram the cross:

 $YYrr \times yy RR \rightarrow \text{all } YyRr \rightarrow 9/16 Y-R-\text{ (yellow round)}: 3/16 Y-rr$  (yellow wrinkled): 3/16 yyR- (green round): 1/16 yyrr (green wrinkled)

Each  $F_2$  pea results from a separate fertilization and so a pod may have peas of different phenotypes. The probability of 7 yellow round  $F_2$  peas is  $(9/16)^7 = 4,782,969/268,435,456 \approx 0.018$ .

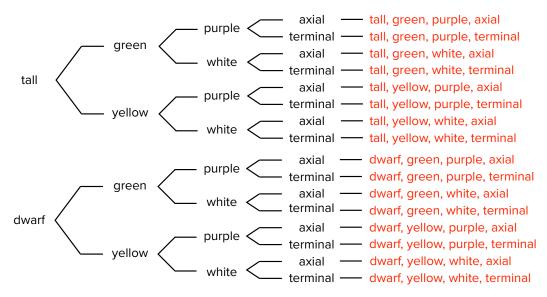
**25.** a. First diagram the cross, and then figure out the progeny ratios for each gene:

```
Aa Tt \times Aa \ Tt \rightarrow 3/4 \ A– (achoo): 1/4 aa (non-achoo) and 3/4 T– (trembling): 1/4 tt (non-trembling)
```

The probability that a child will be A- (and have achoo syndrome) is independent of the probability that it will lack a trembling chin, so the probability of a child with achoo syndrome but without trembling chin is 3/4 A-  $\times$  1/4 tt = 3/16.

**b.** The probability that a child would have neither dominant characteristic is 1/4  $aa \times 1/4$  tt = 1/16.

- **26.** The  $F_1$  must be heterozygous for all the genes because the parents were pure breeding (homozygous). The appearance of the  $F_1$  establishes that the dominant characters for the four traits are tall, purple flowers, axial flowers and green pods.
  - $\mathbf{Q}$ . If you cross two heterozygous  $\mathbf{F}_1$ , both dominant and recessive characters for each trait will appear among the progeny. Thus, you expect  $2 \times 2 \times 2 \times 2 = 16$  different phenotypes when considering the four traits together. The possibilities can be determined using the product rule with the pairs of characters for each gene, because the traits are inherited independently. Thus: [tall: dwarf] × [green: yellow] gives [tall green: tall yellow: dwarf green: dwarf yellow] × [purple: white] gives [tall green purple: tall yellow purple: dwarf green purple: dwarf yellow purple: tall green white : tall yellow white : dwarf green white : dwarf yellow white] × [terminal : axial] which gives (i) tall green purple terminal: (ii) tall yellow purple terminal: (iii) dwarf green purple terminal: (iv) dwarf yellow purple terminal: (v) tall green white terminal: (vi) tall yellow white terminal: (vii) dwarf green white terminal: (viii) dwarf yellow white terminal: (ix) tall green purple axial: (x) tall yellow purple axial: (xi) dwarf green purple axial: (xii) dwarf yellow purple axial: (xiii) tall green white axial: (xiv) tall yellow white axial: (xv) dwarf green white axial: (xvi) dwarf yellow white axial. The possibilities can also be determined using a branchedline diagram:



**b.** Designate the alleles: T = tall, t = dwarf; G = green; g = yellow; P = purple, p = white; A = axial, a = terminal. The cross Tt Gg Pp Aa (an  $F_1$  plant)  $\times tt gg pp AA$  (the dwarf parent) will produce 2 characters for the tall, green and purple genes, but only 1 character (axial) for the fourth gene or  $2 \times 2 \times 2 \times 1 = 8$  different phenotypes. The first 3 genes will give 1 dominant: 1 recessive ratios of the characters, because this is in effect a testcross for each gene. Thus, the proportion of each phenotype in the progeny will be  $1/2 \times 1/2 \times 1/2 \times 1/2 \times 1/8$ .

Using either of the methods described in part (a), the progeny will be 1/8 tall green purple axial: 1/8 tall yellow purple axial: 1/8 dwarf green purple axial:

1/8 dwarf yellow purple axial: 1/8 tall green white axial: 1/8 tall yellow white axial: 1/8 dwarf green white axial: 1/8 dwarf yellow white axial.

- 27. For each separate cross, determine the number of genes involved. Remember that the existence of 4 phenotypic classes in the progeny means that 2 genes control the phenotypes. Next, determine the phenotypic ratio for each gene separately. A 3:1 phenotypic ratio of progeny tells you which character is dominant and that both parents were heterozygous. In contrast, a 1:1 ratio results from a testcross where the dominant parent was heterozygous.
  - C1. Two genes with alternate alleles are at play in this cross (four phenotypes). One gene controls flower color (purple or white) with a phenotypic ratio in the offspring of 94 + 28 = 122 purple : 32 + 11 = 43 white or ~3 purple : ~1 white. The second gene controls pod texture (spiny or smooth) with a phenotypic ratio in the offspring of 94 + 32 = 126 spiny : 28 + 11 = 39 smooth or ~3 spiny : ~1 smooth. Thus, designate the alleles P = purple, p = white; S = spiny, s = smooth. This is a straightforward dihybrid cross: Pp Ss × Pp Ss → 9 P-S-: 3 P-ss: 3 pp S-: 1 pp ss.
  - b. The 1 spiny: 1 smooth ratio indicates a testcross for the pod texture gene. Because all progeny were purple, at least one parent plant must have been homozygous for the *P* allele of the flower color gene. The cross was either *PP Ss* × *P- ss* or *P- Ss* × *PP ss*.
  - **C.** This row is similar to part (b), but here all the progeny were spiny so at least one parent must have been homozygous for the S allele. The 1 purple : 1 white testcross ratio indicates that the parents were either  $Pp S \times pp SS$  or  $Pp SS \times pp S \cdot$ .
  - **d.** For color, there are 89 + 31 = 120 purple: 92 + 27 = 119 white. A 1 purple: 1 white ratio denotes a testcross. For texture, there are 89 + 92 = 181 spiny: 31 + 27 = 58 smooth, or a 3 spiny: 1 smooth ratio, indicating that the parents were both heterozygous for the *S* gene. The genotypes of the parents were *Pp Ss* × *pp Ss*.
  - **e.** A 3 purple : 1 white ratio exists among the progeny, so the parents were both heterozygous for the P gene. All progeny had smooth pods, so the parents were both homozygous recessive ss. The genotypes of the parents are  $Pp ss \times Pp ss$ .
  - f. A 3 spiny: 1 smooth ratio exists, indicative of a cross between heterozygotes  $(Ss \times Ss)$ . All progeny were white, so the parents must have been homozygous recessive pp. The genotypes of the parents are  $pp Ss \times pp Ss$ .
- **28.** Three traits (each controlled by a different gene) are analyzed in this cross. While we can usually tell which alleles are dominant from the phenotype of the heterozygote, we are not told the phenotype of the heterozygote in this case. Instead, use the phenotypic ratios for each trait to determine which allele is dominant and which is recessive for each gene. Consider height first. There are 272 + 92 + 88 + 35 = 487 tall plants and 93 + 31 + 29 + 11 = 164 dwarf plants. This is a ratio of ~3 tall: ~1 dwarf, indicating that **tall is dominant**. Next consider pod shape, where there are 272 + 92 + 93 + 31 = 488 inflated pods and 88 + 35 + 29 + 11 = 163 flat pods, or approximately 3 inflated: 1 flat, so **inflated is dominant**. Finally, consider flower color. There were 272 + 88 + 93 + 29 + 11 = 493

purple flowers and 92 + 35 + 31 + 11 = 169 white flowers, or ~3 purple : ~1 white. Thus, **purple is dominant**.

**29.** Diagram each of these crosses, remembering that you were told that tiny wings = t, normal wings = T, narrow eye = n, and oval (normal) eye = N. You thus know that one gene determines the wing trait and a different gene determines the eye trait, and you also know the dominance relationship between the alleles of each gene.

In cross 1, all of the parents and offspring have tiny wings so no variability exists in the wing gene, and all flies in this cross are tt. Note that although both parents have oval eyes (N-), the eyes in the offspring are ~3 oval : ~1 narrow. This monohybrid phenotypic ratio means that both parents are heterozygous for the eye gene (Nn). Thus, **the parents in cross 1 are:**  $tt \, Nn \, 3 \times tt \, Nn \, 9$ .

In cross 2 consider the wings first. The male parent has normal wings (T-), and the female parent has tiny wings (tt) so this is a testcross. The offspring show a ratio of ~1 tiny: ~1 normal. Therefore, the normal male parent must be heterozygous (Tt). For eyes, the female parent is oval (N-) the male parent is narrow (nn) so this is a testcross for the eye gene. The offspring are ~1 oval: ~1 narrow, so the oval female parent is an Nn heterozygote. Thus, parents in cross 2 are:  $Tt nn d \times tt Nn Q$ .

In cross 3, the parents both have normal wings (T-) and their offspring are ~3 normal: ~1 tiny. Thus, both parents are Tt heterozygotes. For the eye gene, the female parent is oval (N-) and the male parent is narrow (nn), so cross 3 is a testcross. Both eye types are seen in the offspring in a ~1 normal: ~1 narrow ratio, so the female parent is heterozygous (Nn). The parents in cross 3 are:  $Tt \, nn \, d \times Tt \, Nn \, Q$ .

When examining cross 4 you notice a monohybrid phenotypic ratio in the offspring of ~3 normal : ~1 tiny for the wings. Thus, both normal-winged parents are Tt. Because the female parent has normal eyes (N-) and the male parent has narrow eyes (nn), this cross is a testcross for the eye gene. All the progeny have oval eyes, so the female parent must be homozygous NN. Thus, the parents in cross 4 are:  $Tt \, nn \, d \times Tt \, NN \, Q$ .

- **30. a.** Analyze each gene separately:  $Tt \times Tt$  will give 3/4 T- (normal wing) offspring. The cross  $nn \times Nn$  will give 1/2 N- (normal eye) offspring. To calculate the probability of the normal offspring, apply the product rule to the normal portions of the ratios by multiplying these two fractions: 3/4  $T- \times 1/2$  N- = 3/8 T- N-. Thus, 3/8 of the offspring of this cross will have normal wings and oval eyes.
  - **b.** Diagram the cross:

$$Tt \ nn \ Q \times \ Tt \ Nn \ \ \ \ \ \ ?$$

First, find the phenotypic ratio in the offspring separately for each gene. A cross of  $Tt \times Tt \rightarrow 3/4$  T– (normal wings): 1/4 tt (tiny wings). For the eyes the cross is  $nn \times Nn \rightarrow 1/2$  N– (oval): 1/2 nn (narrow). Second, applying the product rule gives 3/8 T– N– (normal oval): 3/8 T– nn (normal narrow): 1/8 tt N– (tiny oval): 1/8 tt nn (tiny narrow). Finally, multiply each fraction by 200 progeny to find the expected ratio, which is **75 normal oval**: **75 normal narrow**: **25 tiny oval**: **25 tiny narrow**.

31. a. The protein specified by the pea color gene is an enzyme called Sgr, which is required for the breakdown of the green pigment chlorophyll. (See Fig. 1.17b.)

- **b.** The *y* allele could be a null allele because it does not specify the production of any of the Sgr enzyme.
- **C.** The *Y* allele is dominant because in the heterozygote, the single *Y* allele will lead to the production of some Sgr enzyme, even though the *y* allele cannot specify any Sgr. The amount of the Sgr enzyme made in heterozygotes is sufficient for yellow color.
- **d.** In *yy* peas, the green chlorophyll cannot be broken down, so this pigment stays in the peas, which remain green in color.
- **e.** If the amount of Sgr protein is proportional to the number of functional copies of the gene, then YY homozygotes should have twice the amount of Sgr protein as do Yy heterozygotes. Yet both YY and Yy peas are yellow. These observations suggest that half the normal amount of Sgr enzyme is sufficient for the pea to break down enough chlorophyll that the pea will be yellow.
- f. Just as was seen in part (e), for many genes (including that for pea color), half the amount of the protein specified by the gene is sufficient for a normal phenotype. Thus, in most cases, even if the gene is essential, heterozygotes for null alleles will survive. The advantage of having two copies of essential genes is then that even if one normal allele becomes mutated (changed) so that it becomes a null allele, the organism can survive because half the normal amount of gene product is usually sufficient for survival.
- **g.** Yes, a single pea pod could contain peas with different phenotypes because a pod is an ovary that contains several ovules (eggs), and each pea represents a single fertilization event involving one egg and one sperm (from one pollen grain). If the female plant was *Yy* or *yy*, then it is possible that some peas in the same pod would be yellow and others green. For example, fertilization of a *y* egg with *Y* sperm would yield a yellow pea, but if the sperm was *y*, the pea would be green. However, a pea pod could not contain peas with different phenotypes if the female plant was *YY*, because all the peas produced by this plant would be yellow.
- h. Yes, it is possible that a pea pod could be different in color from a pea growing within it. One reason is that, as just seen in part (g), a single pod can contain green and yellow peas. But a more fundamental reason is that one gene controls pea color, while a different gene controls the pod color. (See Fig. 1.5.)
- **32.** If the alleles of the pea color and pea shape genes inherited from a parent in the P generation always stayed together and never separated, then the gametes produced by the doubly heterozygous  $F_1$  individuals in Fig. 1.12 would be either YR or yr. (Note that only two possibilities would exist, and these would be in equal frequencies.) On a Punnett square (male gametes shaded in blue, female gametes in red):

	YR	y r
	1/2	1/2
YR	YY RR	Yy Rr
1/2	1/4	1⁄4
y r	Yy Rr	yy rr
1/2	1/4	1⁄4

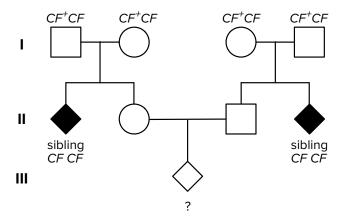
Thus, the genotypic ratios of the  $F_2$  would be 1/4 YY RR, 1/2 Yy Rr, and 1/4 yy rr. The phenotypic ratios among the  $F_2$  would be 3/4 yellow round and 1/4 green wrinkled. These results make sense because if the alleles of the two genes were always inherited as a unit, you would expect the same ratios as in a monohybrid cross.

- 33. Similar to what you saw in Fig. 1.17, the most likely biochemical explanation is that the dominant allele *L* specifies functional G3βH enzyme, while the recessive allele *I* is incapable of specifying any functional enzyme (in nomenclature you will see in later chapters, *I* is a *null allele*). The functional enzyme can synthesize the growth hormone gibberellin, so plants with the *L* allele are tall. Even half the normal amount of this enzyme is sufficient for tallness, explaining why *LI* heterozygotes are tall.
- **34. a.** As in Problem 33, the dominant allele *P* most likely specifies a functional product (in this case, the protein bHLH), while the recessive *p* allele cannot specify any functional protein. The fact that the hybrid (the heterozygote) is purple (as shown in Fig. 1.5) indicates that half the normal amount of active bHLH protein is sufficient for purple color.
  - **b.** Yes, flower color could potentially be controlled by genes specifying the enzymes DFR, ANS, or 3GT in addition to the gene specifying the bHLH protein. Alleles specifying functional enzymes would yield purple color, while those that could not produce functional enzymes would cause white color. From the reasoning in part (a), it is likely that the purple alleles of these genes would be dominant to the white alleles.

#### Section 1.3

- **35.** To clarify which are the dominant and recessive alleles, in answering this question, we are using Mendelian symbols instead of the symbols normally used for human genotypes.
  - **G.** Recessive. Two unaffected (and consanguineous) individuals have an affected child (aa). Therefore, the parents involved in the consanguineous marriage must both be carriers (Aa). In addition, II-1 and V-2 are affected (aa); all unaffected individuals except II-2, II-4, III-5, and possibly V-1 are carriers (Aa).
  - **b.** Dominant. The trait is seen in each generation and every affected person (A-) has an affected parent. Note that III-3 is unaffected (aa) even though both his parents are affected; this would not be possible for a recessive trait. The term *carrier* is not applicable, because everyone with a single A allele shows the trait. All affected individuals are Aa, except III-4, III-5, and III-6 could be AA (that is, the latter three individuals are A-).

- **C.** Recessive. Unaffected, carrier parents (Aa) have an affected child (aa), as in part (a). I-2 and III-4 are affected (aa); everyone in generation II is a carrier (Aa); III-1, III-2, and III-3 could be either AA or Aa; I-1 is almost certainly AA if the disease is rare.
- **36.** *a.* Cutis laxa must be a recessive trait because affected child II-4 has normal parents. II-4 is affected, so she must have received a disease allele (CL) from both parents. The mother (I-3) and the father (I-4) are both heterozygous ( $CL^+CL$ ).
  - **b.** The mother of II-2 is affected and therefore is of genotype CL CL (I-1). II-2 herself does not have cutis laxa, but she must have received a CL allele from her mother. Therefore, II-2's genotype must be  $CL^+CL$ , meaning that **the probability that II-2 is a carrier is 100%**.
  - C. As described in part (a) both parents in this cross are carriers:  $CL^+ CL \times CL^+ CL$ . The expected genotypic ratio in the children is 1  $CL^+ CL^+ : 2 CL^+ CL : 1 CL CL$ . However, II-3 is <u>not</u> affected, so he cannot be CL CL. Therefore, the remaining possibilities are 1  $CL CL^+ : 2 CL^+ CL$ , and so a 1/3 probability exists that he is  $CL^+ CL^+$ , while a 2/3 probability exists that he is a carrier ( $CL^+ CL$ ).
  - **d.** As shown in part (b), II-2 must be a carrier ( $CL^+CL$ ). In order to have an affected child, II-3 must also be a carrier. The probability of this is 2/3 as shown in part (c). The probability of two heterozygous parents having an affected child is 1/4. Apply the product rule to these probabilities: 1 (probability that II-2 is  $CL^+CL$ ) × 2/3 (probability that II-3 is  $CL^+CL$ ) × 1/4 (probability of an affected child from a mating of two carriers) = 2/12 = 1/6.
- **37.** Diagram the cross as a pedigree. Remember that the affected siblings must be *CF CF*.



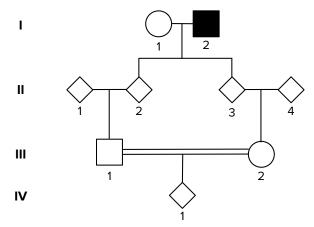
**G.** Both families have an affected sibling, so both sets of parents (that is, all the people in generation I) must have been carriers. Thus, the expected genotypic ratio in the children is 1/4 affected: 1/2 carrier: 1/4 homozygous normal. II-2 is unaffected, so she cannot be CF CF. The remaining possible genotypes are 2 CF + CF + CF and the probability is 2/3 that II-2 is a carrier.

- **b.** The probability that II-2 × II-3 will have an affected child is 2/3 [the probability that the mother is a carrier as seen in part (a)] × 2/3 (the probability the father is a carrier using the same reasoning) × 1/4 (the probability that two carriers will produce an affected child) = 1/9.
- C. The probability that both parents are carriers and that their child will be a carrier is  $2/3 \times 2/3 \times 1/2 = 2/9$  [using the same reasoning as in part (b), except asking that the child be a carrier instead of affected]. However,  $CF^+CF^+ \times CF^+ CF$  parents can also have children who are carriers. Remember that there are two possible ways for this particular mating to occur: homozygous father  $\times$  heterozygous mother or vice versa. Thus, the probability of one of these matings producing a carrier child is:  $2 \times 1/3$  (the probability that a particular parent is  $CF^+CF^+$ )  $\times$  2/3 (the probability that the other parent is  $CF^+CF \times 1/2$  (the probability such a mating would produce a carrier child) = 2/9. The probability that a child would be a carrier from either of these two scenarios (where both parents are carriers or where only one parent is a carrier) is the sum of these mutually exclusive events, or 2/9 + 2/9 = 4/9.
- **38.**  $\sigma$ . Because the disease is rare, the affected father is most likely to be heterozygous  $(HD\ HD^+)$ . A 1/2 chance exists that the son inherited the HD allele from his father and will develop the disease.
  - **b.** The probability of an affected child is: 1/2 (the probability that Joe is  $HD HD^+$ ) × 1/2 (the probability that the child inherits the HD allele if Joe is  $HD HD^+$ ) = 1/4.
- 39. The trait is recessive because pairs of unaffected individuals who must therefore be carriers (I-1  $\times$  I-2 as well as II-3  $\times$  II-4) had affected children (II-1, III-1, and III-2). Three apparently unrelated individuals must have been carriers (I-1, I-2, and II-4), so the disease allele appears to be common in the population.
- **40. a.** The inheritance pattern seen in Fig. 1.19 could be caused by a rare dominant mutation. In this case, the affected individuals would be heterozygous ( $HD^+HD$ ) and the normal individuals would be  $HD^+HD^+$ . Any mating between an affected individual and an unaffected individual would give 1/2 normal ( $HD^+HD^+$ ): 1/2 affected ( $HD^+HD$ ) children. However, the same pattern of inheritance could be seen if the disease were caused by a common recessive mutation. In the case of a common recessive mutation, all the affected individuals would be HDHD. Because the mutant allele is common in the population, most or even all the unrelated individuals could be assumed to be carriers ( $HD^+HD$ ). Matings between affected and unaffected individuals would then also yield phenotypic ratios of progeny of 1/2 normal ( $HD^+HD$ ): 1/2 affected (HDHD).
  - **b.** Determine the phenotype of the 14 children of III-6 and IV-6. If the disease is due to a recessive allele, then III-6 and IV-6 must be homozygotes for this recessive allele, and all their children must have the disease. If the disease is due to a dominant allele, then III-6 and IV-6 must be heterozygotes (because they are affected but they each had one unaffected parent), and 1/4 of their 14 children would be expected to be unaffected.

Alternatively, you could look at the progeny of matings between unaffected individuals in the pedigree such as III-1 and an unaffected spouse. If the disease were due to a rare dominant allele, these matings would all be homozygous recessive × homozygous recessive and would never result in affected children. If the disease is due to a recessive mutation, then many of these individuals would be carriers, and if the trait is common then at least some of the spouses would also be carriers, so such matings could result in affected children.

- **41. a.** For the couple in generation V in Fig. 1.21a to have a child with cystic fibrosis, both of them would have to be carriers, meaning that they would both have to have inherited the CF allele from their great-great-grandfather or great-great-grandmother in generation I. The chance that V-1 inherited the CF allele is: 1/2 (the chance that II-2 inherited CF) × 1/2 (the chance of III-2 inheriting CF if II-2 was a carrier) × 1/2 (the chance of IV-2 inheriting CF if IV-2 was a carrier) = 1/16. Using the same logic, the chance that V-2 inherited the CF allele is also 1/16. Thus, the chance that their child would be CFCF is  $1/16 \times 1/16 \times 1/4$  (the chance that they both give the CF allele to their child given that they are both carriers) = 1/1024. The consanguineous couple in Fig. 1.21a was thus extremely unlucky in this outcome for their child.
  - **b.** Knowing that VI-4 has cystic fibrosis simplifies this problem because we know definitively that V-1 and V-2 are both carriers. The likelihood of VII-1 having the disease depends on the chance that both of his parents are carriers. The chance that her mother (VI-2) is a carrier is 2/3. The reason is that both V-1 and V-2 are carriers, so their expected progeny ratio is  $1 \ CF^+CF^+: 2 \ CF^+CF: 1 \ CF \ CF$ . However, we know that VI-2 is not  $CF \ CF$  (she is unaffected), which leaves  $1 \ CF^+CF^+: 2 \ CF^+CF$ , or a 2/3 chance that VI-2 is  $CF^+CF$ . The chance that her father (VI-1) is  $CF^+CF$  is 1/1000. Thus, given the problem's assumptions, the chance that VII-1 would have cystic fibrosis is  $2/3 \times 1/1000$  (the chance that both her parents are carriers)  $\times 1/4$  (the chance that she inherits CF from both parents) = 1/6000.

## **42.** $\alpha$ . The pedigree diagram that describes this situation is:



We'll use Mendelian symbols as opposed to the symbols normally used for human genes here to clarify which are the dominant and which are the recessive alleles. Let's designate *a* the symbol for the recessive disease allele carried by the common grandfather (I-1) of the first cousins (III-1 and III-2), and *A* the normal allele. Similarly, let *b* be the symbol for the recessive disease allele carried by their common grandmother (I-2), with the normal allele *B*. The question is: what is the chance that the child of the first cousins (IV-1) would be either *aa* or *bb*?

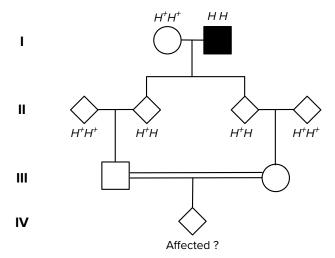
For IV-1 to be aa, both first cousins (III-1 and III-2) have to be Aa, which means that II-2 and II-3 must also both be Aa. The chance that II-2 inherited the a allele from I-1 is 1/2, and the chance that II-3 inherited the a allele from I-2 is also 1/2. Given that II-2 and II-3 are Aa, the chance that III-1 inherited II-2's a allele is 1/2, and the chance that III-2 inherited II-3's a allele is 1/2. For both first cousins to be Aa, all of these conditions must be met, and so the probability that both first cousins are Aa is  $1/2 \times 1/2 \times 1/2 \times 1/2 = 1/16$ . As the expected frequency of aa from a cross of  $Aa \times Aa$  is 1/4, the chance that the child of the first cousins will be aa is  $1/16 \times 1/16 = 1/166$ . By the same logic, the chance that their child will be aa is aa or aa

The exact answer is a bit less because our calculation of the probability of IV-1 being aa included the chance of the child being aa bb. So did our calculation of the chance that IV-2 is bb. Therefore, we need to subtract one of those aa bb chances. The probability that the child is aa bb is  $1/64 \times 1/64 = 1/4096$ . Thus, a more accurate estimate of the chance that the child is aa or bb is  $1/32 - 1/4096 \approx 1/32.25$ .

**b.** This is a really hard question, but we asked it because it's interesting to think about whether it makes sense, on genetic grounds, for first cousin marriages to be banned, which is the subject of part (c). Also, if you remember how to answer questions like this one, you will be a very powerful genetics problem solver!

The chance that two random people have the same disease allele is  $1/6,000 \times$ 1/6,000 = 1/36,000,000. And if they do, the chance that their child will be homozygous is 1/4. Thus, the overall chance of two random people having a child homozygous for a recessive disease allele for any 1 of the 6000 disease genes is  $1/4 \times 1/36,000,000 =$ 1/144,000,000. The chance that the child would *not* be homozygous for a specific one of the 6,000 recessive genetic disease alleles is 1-(1/144,000,000) =143,999,999/144,000,000. (The reason is that a person is either homozygous for a particular allele or they are not—those are the only two choices; the sum of their probabilities equals 1.) The chance that their child would *not* be homozygous for a recessive disease allele at *any one* of the 6,000 loci is  $(143,999,999/144,000,000)^{6000}$ . (You use the product rule to determine the chance that this event happens 6000 times.) Finally, the chance that a person would be homozygous for at least one recessive disease allele is  $1 - (143,999,999/144,000,000)^{6000} = 0.00004167 = 1/23,998$ . (The reason is that every person is either homozygous for no disease gene alleles, or for at least 1—those are the only two choices and so the sum of their probabilities is 1.)

- C. We calculated in part (a) that the chance is  $\sim 1/32$  that first cousins would have a child homozygous for a recessive disease allele, which is much higher than the risk for two random individuals ( $\sim 1/24,000$ ). However, because only a small fraction of birth defects is caused by homozygosity for recessive alleles, the overall chance of serious defects at birth for any child in the U.S. is estimated to be as high as 3/100. Thus, it would appear that **first-cousin parents do not have much of an overall increased risk of having children with birth defects** (1/32 = 3/96, which is close to 3/100). (We are assuming that the fraction of first-cousin parents among all the parents in the U.S. is tiny, and that the children of first-cousin parents do not have a higher tendency than unrelated parents to have congenital birth defects with nongenetic causes.)
- **43.** Diagram the cross by drawing a pedigree:



- **G.** Assuming the disease is rare, the first generation is  $H^+H^+$  unaffected (I-1)  $\times$  HH affected (I-2). Thus, both children (II-2 and II-3) must be carriers ( $H^+H$ ). Again, assuming this trait is rare in the population, those people marrying into the family (II-1 and II-4) are homozygous normal ( $H^+H^+$ ). Therefore, the probability that III-1 is a carrier is 1/2; III-2 has the same chance of being a carrier. Thus, the probability that a child produced by these two first cousins would be affected is 1/2 (the probability that III-1 is a carrier)  $\times$  1/2 (the probability that III-1 is a carrier)  $\times$  1/4 (the probability the child of two carriers would have an HH genotype) = 1/16 = 0.0625.
- **b.** If 1/10 people in the population are carriers, then the probability that II-1 and II-4 are  $H^+H$  is 0.1 for each. In this case an affected child in generation IV can only occur if III-1 and III-2 are both carriers. III-1 can be a carrier as the result of 2 different matings: (i) II-1 homozygous normal  $\times$  II-2 carrier or (ii) II-1 carrier  $\times$  II-2 carrier. [Note that whether I-1 is  $H^+H^+$  or  $H^+H$ , II-2 must be a carrier because of the normal phenotype (II-2 cannot be HH) and the fact that one parent was affected.] The probability of III-1 being a carrier is thus the probability of mating (i)  $\times$  the probability of generating a  $H^+H$  child from mating (i) + the probability of mating (ii)  $\times$

the probability of generating an  $H^+H$  child from mating (ii) = 0.9 [the probability II-1 is  $H^+H^+$ , which is the probability for mating (i)] × 1/2 [the probability that III-1 will inherit H in mating (i)] + 0.1 [the probability II-1 is H, which is the probability for mating (ii)] × 2/3 [the probability that III-1 will inherit H in mating (ii); remember that III-1 is known not to be HH] = 0.45 + 0.067 = 0.517. The chance that III-2 will inherit H is the same. Thus, the probability that IV-1 is HH = 0.517 (the probability III-1 is  $H^+H$ ) × 0.517 (the probability that III-2 is  $H^+H$ ) × 1/4 (the probability the child of two carriers will be HH)  $\approx$  0.067. This number is slightly higher than the answer to part (a), which was 0.0625, so the increased likelihood that II-1 or II-4 is a carrier makes it only slightly more likely that IV-1 will be affected.

The results of this problem should prove to you that in probability calculations involving the outcomes of consanguineous matings, it makes sense to assume that people in the diagram who are unrelated genetically to the person who introduced a recessive disease allele are homozygous for the normal allele (not carriers). You just saw that when you take into account a 1/10 chance that these unrelated people are carriers, it did not change very much your probability calculation. The frequency of recessive disease allele carriers in most populations is usually orders of magnitude lower than 1/10, so taking these possibilities into account is unlikely to change your calculation at all. It is usually overwhelmingly more likely that related individuals who are both carriers of recessive disease alleles each inherited the allele from their common ancestor than that each of their disease alleles had different sources.

- 44. a. Both diseases are known to be rare, so normal people in the pedigree unrelated genetically to I-1 or I-2 are assumed to be homozygous normal. (Again, we are using Mendelian symbols as opposed to human genetics symbols here to clarify which alleles are dominant and which are recessive.) Nail-patella (N) syndrome is dominant because all affected children have an affected parent. Alkaptonuria (a) is recessive because the affected children are the result of a consanguineous mating between two unaffected individuals (III-3 × III-4). Because alkaptonuria is a rare disease, it makes sense to assume that III-3 and III-4 inherited the same a allele from a common ancestor. Genotypes: I-1 nn Aa; II-2 Nn AA (or I-1 nn AA and I-2 Nn Aa); II-1 nn AA; III-2 nn Aa; III-3 Nn A-; II-4 nn A-; III-5 Nn Aa; III-6 nn AA; III-1 nn AA; III-2 nn A-; III-3 nn Aa; III-4 Nn Aa; III-5 nn A-; III-6 nn A-; IV-1 nn A-; IV-2 nn A-; IV-3 Nn A-; IV-4 nn A-; IV-5 Nn aa; IV-6 nn aa; IV-7 nn A-.
  - b. The cross is  $nn\ A-$  (IV-2)  $\times\ Nn\ aa$  (IV-5). The ambiguity in the genotype of IV-2 is due to the uncertainty of his father's genotype (III-2). His parents' genotypes are  $nn\ AA$  (II-1)  $\times\ nn\ A-$  (II-2), so there is a 1/2 chance III-2 is  $nn\ AA$  and a 1/2 chance he is  $nn\ Aa$ . If he is  $nn\ Aa$ , there is a 1/2 chance IV-2 would have inherited his a allele. Therefore, the overall chance that IV-2 is  $nn\ Aa$  is  $1/2 \times 1/2 = 1/4$ , and the chance that IV-2 is  $nn\ AA$  is 3/4.

For the child to have both syndromes (N-aa), IV-2 would have to be nn Aa. The cross would then be nn  $Aa \times Nn$  aa, and the chance of an N-aa child from this cross is  $1/2 \times 1/2 = 1/4$ . Thus, the chance that the child would be N-aa is 1/4 (the chance that IV-2 is nn Aa)  $\times$  1/4 = 1/16.

The child can have nail-patella syndrome only (N-A-) if IV-2 is nnAa or nn AA. If the cross is nn  $Aa \times Nn$  aa, the chance that the child would be N-A- (Nn Aa) is  $1/2 \times 1/2 = 1/4$ . If the cross is nn  $AA \times Nn$  aa, the chance that the child is Nn Aa is  $1/2 \times 1 = 1/2$ . We need to use weighted probability to determine the chance that the child is Nn Aa: [1/4 (the chance that IV-2 is nn Aa)  $\times$  1/4] + [3/4 (the chance that IV-2 is nn AA)  $\times$  1/2] = 1/16 + 3/8 = 7/16.

For the child to have alkaptonuria only (nn aa), IV-2 must be nn Aa; the cross would be nn  $Aa \times Nn$  aa. The probability of an nn aa child from this cross is  $1/2 \times 1/2 = 1/4$ . Thus, the chance that the child would be nn aa is 1/4 (the chance that IV-2 is nn Aa)  $\times$  1/4 = 1/16.

The probability that the child would have neither defect is 1 - [P(only alkaptonuria) + P(only nail-patella syndrome) + P(both defects)] = <math>1 - (1/16 + 7/16 + 1/16) = 1 - 9/16 = 7/16. You can make this calculation because only the four possible outcomes exist, and you have already calculated the probabilities of three of them.

## **45.** Diagram the cross(es):

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midphalangeal \times midphalangeal \rightarrow 1853 midphalangeal : 209 normal M? \times M? \rightarrow M? : M^+M^+
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The following crosses are possible:

$$MM^+$$
  $\times$   $MM$   $\rightarrow$  all  $MM$   
 $MM^+$   $\times$   $MM$   $\rightarrow$  all  $-$   
 $MM$   $\times$   $MM^+$   $\rightarrow$  all  $-$   
 $MM^+$   $\times$   $MM^+$   $\rightarrow$   $3/4 M-: 1/4 M^+M^+$ 

The 209 normal children must have arisen from the last cross, so approximately  $3 \times 209 \approx 630$  children should be their M- siblings. Thus, about 840 of the children or ~40% came from the last mating and the other 60% of the children (all of whom have midphalangeal hair) were the result of one or more of the other matings. This problem illustrates that much care in interpretation is required when the results of many matings in mixed populations are reported (as opposed to the results of matings where individuals have defined genotypes).

- **46. a.** An equally likely possibility exists that any child produced by this couple will be affected (A) or unaffected (U). For two children, the possibilities are: AA, AU, UA, UU. The case in which only the second child is affected is UA; this is one of the four equally likely possibilities, so the probability that only the second child is affected is 1/4.
  - **b.** From the list just presented in part (a), you can see that two possibilities exist in which only one child is affected: AU and UA. The probability that either of these two mutually exclusive possibilities will occur is the sum of their independent probabilities: 1/4 + 1/4 = 1/2.
  - **C.** From the list just presented in part (a), you can see that only one possibility exists in which no child is affected: UU. The probability of this event is **1/4**.

d. If this family consisted of 10 children, the case in which only the second child out of the 10 is affected (that is, UAUUUUUUUU) has a probability of  $1/2^{10} = 1/1024 \approx 0.00098$ . This probability is based on the facts that each birth is an independent event, and that the chance of U and A are each 1/2. We thus use the product rule to determine the chance that each of those 10 independent events will occur in a particular way—one particular birth order.

In a family of ten children, 10 different outcomes (birth orders) exist that satisfy the criterion that only 1 child has the disease. Only the first child could have the disease, only the second child, only the third child, etc.:

- 1. AUUUUUUUU
- 2. UAUUUUUUU
- 3. UUAUUUUUU
- 4. UUUAUUUUUU
- 5. UUUUAUUUUU
- 6. UUUUUAUUUU
- 7. UUUUUUAUUU
- 8. UUUUUUUAUU
- 9. UUUUUUUUAU
- 10. UUUUUUUUA

We have already calculated that the chance of one of these outcomes in particular (#2) is 1/1024. As each of the 10 possibilities has the same probability, the probability that only one child is affected would be  $10 \times (1/1024) = 10/1024 \approx 0.0098$ .

Only one possibility exists in which no child would be affected (UUUUUUUUUU), and like any other specific outcome, this one has a probability of  $1/1024 \approx 0.00098$ .

- **e.** One way to determine the probability that four children in a family of ten will have the disease is to write down all possible outcomes for the criterion, as we did above for the second answer in part (d). Then, also as we did above, sum their individual probabilities, each of which is  $(1/2)^{10}$  just as before. If you start to do this......
  - 1. AAAAUUUUUU
  - 2. AAAUAUUUUU
  - 3. AAAUUAUUUU
  - 4. AAAUUUAUUU
  - 5. AAAUUUUAUU
  - 6. AAAUUUUUAU
  - 7. AAAUUUUUUA
  - 8. AAUAAUUUUU
  - 9. AAUAUAUUUU
  - 10. AAUAUUAUUU

etc.

.....you will realize fairly quickly that writing down every possible birth order in this case is quite a difficult task and you are likely to miss some outcomes. In short—this is not a good way to find the answer! For questions like this, it is far preferable to use a mathematical tool called the **binomial theorem** to determine the number of possible outcomes that satisfy the criterion. The binomial theorem looks like this:

P (X will occur s times, and Y will occur t times, in n trials) =  $[n!/(s! \times t!)](p^s \times q^t)$ 

P = the probability of what is in parentheses on the left side of the equation.

p = P(X)

q = P(Y)

**X** and **Y** are the only two possibilities, so p + q = 1.

Also, s + t = n.

Remember that ! means factorial: For example  $5! = 5 \times 4 \times 3 \times 2 \times 1$ 

To apply the binomial theorem to the question at hand (assuming you can still remember what the question was!), we'll let X = a child has the disease (A), and Y = a child does not have the disease (U). Then, S = 4, S = 4, S = 4, S = 4, and S = 4, and S = 4, S = 4

P (4 A and 6 U children out of 10) = 
$$(10! / 4! \times 6!) (1/2^4 \times 1/2^6)$$

Notice that  $(p^s \times q^t) = (1/2^4 \times 1/2^6) = 1/2^{10}$ . This factor of the binomial theorem equation is the probability of each single birth order, as we saw previously in part (d) above. To get the answer to our question, we need to multiply this factor (the probability of each single birth order) by the number of different birth orders that satisfy our criterion. From the equation in the box above, this second factor is  $[n!/(s! \times t!)] = (10! / 4! \times 6!) = 210$ . Thus, the probability (P) of only 4 children having the disease in a family of 10 children is  $1/2^{10} \times 210 \approx 21\%$ .

**47.** In the case of cystic fibrosis, the alleles causing the disease do not specify active protein [in this case, the cystic fibrosis transmembrane receptor (CFTR)]. Some *CF* disease alleles specify defective CFTR proteins that do not allow the passage of chloride ions, while other *CF* disease alleles do not specify any CFTR protein at all. As you will learn in a later chapter, *CF* disease alleles of either type are called *loss-of-function* alleles. In a heterozygote, the normal *CF*<sup>+</sup> allele still specifies active CFTR protein, which allows for the passage of chloride ions. Because the phenotype of heterozygotes is unaffected, these individuals must have enough active CFTR protein to allow passage of enough chloride ions for the cells to function normally. Loss-of-function alleles of most genes are recessive to normal alleles for similar reasons. But it is imperative to realize that important exceptions exist in which loss-of-function mutations are actually dominant to normal alleles; you will see examples of these exceptions later in the book.

In the case of Huntington disease, the disease-causing allele is dominant to the normal allele. The reason is that **the mutant huntingtin protein specified by the** *HD* **disease allele has, in addition to its normal function** (which is not entirely understood),

- a second function that is toxic to nerve cells. This fact makes the HD disease allele a gain-of-function allele. The reason HD is dominant to  $HD^+$  is that the protein specified by the disease allele will be toxic to cells even if the cells have normal huntingtin protein specified by the normal allele. Most (but again not all) gain-of-function mutations are dominant to normal alleles for similar reasons.
- **48.** Like the abnormal *CF* allele that causes cystic fibrosis, the mutant *GLI3* allele that causes polydactyly is a *loss-of-function* allele—it makes no active protein. Unlike the one normal *CF*<sup>+</sup> allele in *CF*<sup>+</sup>*CF* heterozygotes, however, the one normal *GLI3*<sup>+</sup> allele in the *GLI3*<sup>+</sup> *GLI3* heterozygotes does not make enough protein to avoid a mutant phenotype—in the case of *GLI3*, the fingers and toes of heterozygous individuals fail to develop properly. You will learn in a later chapter of this book that genes like *GLI3* are called *haploinsufficient genes*. You have ~800 such genes in your genome, for which the amount of gene product made from one gene copy is not enough for the organism to function normally.

You might be wondering about the phenotype of *GLI3 GLI3* homozygotes. If *GLI3*+ *GLI3* heterozygotes have polydactyly, and *GLI3* is dominant to *GLI3*+, you should expect that *GLI3 GLI3* homozygotes would have polydactyly also. The fact is that the homozygotes die early in development. You will learn in the next chapter that many genes are *pleiotropic*—meaning that they control more than one trait. *GLI3* is a pleiotropic gene; it controls the number of digits, and also aspects of embryonic development that are essential for viability. For the phenotype of viability, *GLI3* is recessive to *GLI3*+. You will see in the next chapter that alleles like *GLI3* are called *recessive lethals*.

- 49. a Recessive traits that are common in the population, like red hair in Scotland, show a vertical pattern of inheritance because recessive allele carriers and even homozygotes from outside the family will likely contribute gametes to every generation. Examples in the pedigree shown are II-1, II-4, and II-6. [Note that not every individual in this pedigree is a product of vertical inheritance (for example, III-12) because red hair is due to a common recessive allele as opposed to a dominant one.]
  - **b.** For IV-1 to have red hair, her mother (III-1) would have to be a carrier, and the chance of that is 40%. If III-1 is a carrier, the cross is Rr (III-1)  $\times rr$  (III-2)  $\rightarrow r-$  (IV-1), and the chance that IV-1 is rr is 1/2. Thus, the chance that child IV-1 will have red hair is  $0.4 \times 1/2 = 0.2 = 20\%$ .
  - C. For IV-2 to have red hair, both III-9 and III-10 must be heterozygous (Rr). You know III-9 is Rr because she does not have red hair but her mother II-4 did (that is, II-4 was rr). Both II-5 and II-6 must be Rr as they do not have red hair and they have a child who does have red hair. So, the chance that III-10 is Rr is 2/3 given that he does not have red hair. (You would expect 1 RR: 2 Rr: 1 rr, but rr is ruled out, leaving 1 RR: 2 Rr.) Thus, the chance that IV-2 has red hair is 1 (chance that III-9 is a heterozygote)  $\times$  2/3 (chance that III-10 is a heterozygote)  $\times$  1/4 (chance that two Rr parents have an rr child) = 1/6.